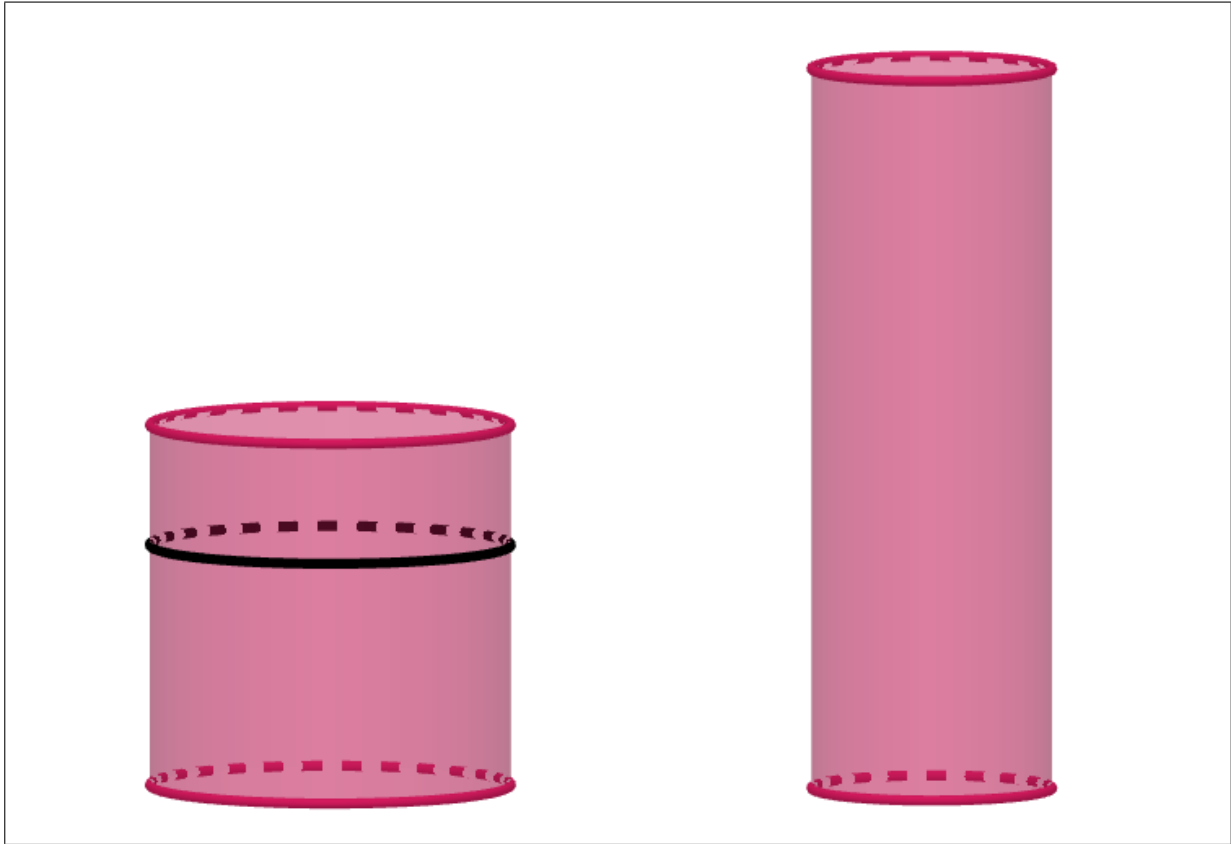


**Problem 1.** The short glass has liquid in it up to the indicated circle. Imagine pouring the liquid into the tall glass.



On the picture of the tall glass, draw a circle which shows how much liquid it will contain after the liquid is poured into the tall glass:

- (a) As perceived by a 3 year old.
- (b) As perceived by a 7 year old.

Think about how an older person may approach this problem, to obtain an exact answer:

- Concretely
- Abstractly

The volume of a cylinder is  $V = Ah = \pi r^2 h$ , where:

- $V$  is the volume
- $A$  is the area of the base of the cylinder
- $r$  is the radius of the circular base
- $h$  is the height of the cylinder

**Problem 2.** Given:

- The short glass has radius 3 and height 6. The liquid in it has height 4.
- The tall glass has radius 2 and height 12.

Compute:

(a) The volume of the liquid in the short glass.

(b) The height of the liquid after it is poured into the tall glass.

**Problem 3.** A cylindrical glass contains a volume  $V = 20\pi$  of liquid up to a height of  $h = 11$ . Find the radius of the glass.

**Problem 4.** Given a cylindrical glass of radius  $r$  containing a volume  $V$  of liquid, find the height of the liquid in terms of  $V$  and  $r$ .